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Measurement of the Ratio of the ν_μ Charged-Current Single-Pion Production to Quasielastic Scattering with a 0.8 GeV Neutrino Beam on Mineral Oil

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Using high statistics samples of charged-current ν_μ interactions, the MiniBooNE Collaboration reports a measurement of the single-charged-pion production to quasielastic cross section ratio on mineral oil (CH_2), both with and without corrections for hadron reinteractions in the target nucleus. The result is provided as a function of neutrino energy in the range $0.4 \text{ GeV} < E_\nu < 2.4 \text{ GeV}$ with 11% precision in the region of highest statistics. The results are consistent with previous measurements and the prediction from historical neutrino calculations.

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Future neutrino oscillation experiments will operate in the 1 GeV energy range, where charged-current quasielastic scattering (CCQE, $\nu_\mu n \rightarrow \mu^- p$) and charged-current single-pion production ($\text{CC}1\pi^+$, $\nu_\mu X \rightarrow \mu^- \pi^+ X'$) are the dominant interactions. Because such processes are the largest contributors to the event samples in such experiments, there has been much interest in making better determinations of their cross sections. At present, the ratio

of $\text{CC}1\pi^+:\text{CCQE}$ cross sections has been measured to $\sim 30\%$ precision based on small event samples [1–3]. A high statistics measurement of these processes necessarily requires the use of nuclear targets where final state interactions obscure the actual value of the ratio of the cross sections on nucleons. Experimentally, it is the cross section on complex nuclei including the effects of final state interactions which is more relevant (experiments can

only identify particles that actually exit the struck nucleus). In this Letter, the MiniNoONE Collaboration reports the first measurement of the observed $CC1\pi^+ : CCQE$ cross section ratio as a function of neutrino energy including the effects of hadronic reinteractions. Additionally, an underlying ratio at the nucleon level is extracted to facilitate comparison with prior measurements [1,3]. Precise knowledge of this cross section ratio is particularly important for future ν_μ disappearance searches, in which $CC1\pi^+$ events typically constitute either a class of signal events or a large background to the CCQE signal. The uncertainty on the $CC1\pi^+ : CCQE$ cross section ratio therefore limits the precision of these measurements.

The Booster Neutrino Beam at Fermilab provides a neutrino source which is particularly well suited to making this measurement; about 40% of ν_μ neutrino interactions in MiniBooNE are expected to be CCQE and 24% $CC1\pi^+$. The beam itself is composed of 93.6% ν_μ with a mean energy of about 800 MeV and 5.9% (0.5%) $\bar{\nu}_\mu$ (ν_e) contamination [4]. The neutrinos are detected in the MiniBooNE detector [5], a 12.2 m diameter spherical tank filled with 818 tons of undoped mineral oil located 541 m downstream of the beryllium target. At the energies relevant to this analysis, the products of the interactions produce primarily Čerenkov light with a small fraction of scintillation light [5]. The light is detected by 1280 8-inch photomultiplier tubes (PMTs) which line the MiniBooNE inner tank. This inner tank region is optically isolated from a surrounding veto region, instrumented with 240 PMTs, that serves to reject incoming cosmic rays and partially contained neutrino interactions.

Neutrino interactions within the detector are simulated with the v3 NUANCE event generator [6]. CCQE interactions on carbon are generated using the relativistic Fermi gas model [7] tuned to better describe the observed distribution of ν_μ CCQE interactions in MiniBooNE [8]. Resonant $CC1\pi^+$ events are simulated using the Rein and Sehgal (R-S) model [9], as implemented in NUANCE with an axial mass $M_A^{1\pi} = 1.1$ GeV. The angular distribution of the decaying pions in the center of mass of the recoiling resonance follows the helicity amplitudes of [9]. In MiniBooNE, 87% of $CC1\pi^+$ production is predicted to occur via the $\Delta(1232)$ resonance, but 17 higher mass resonances and their interferences, as well as a nonresonant background [9] that accounts for roughly 6% of $CC1\pi^+$ events, are also included in the model. Coherently produced $CC1\pi^+$ events are generated using the R-S model [10] with the R-S absorptive factor replaced by NUANCE's pion absorption model and the overall cross section rescaled to reproduce MiniBooNE's recent measurement of neutral current coherent π^0 production [11]. Coherent π^+ production is predicted to compose less than 6% of the MiniBooNE $CC1\pi^+$ sample due to the small coherent cross section [12,13] and the dominance of the Δ^{++} resonance. A GEANT3-based detector model [14]

simulates the response of the detector to particles produced in these neutrino interactions.

To select ν_μ charged-current interactions, simple requirements on the amount of charge detected in the tank (> 175 tank PMT hits) and in the veto region (< 6 veto PMT hits), location of the event in the tank (< 500 cm from the center of the detector), and event time (event must occur while the beam is passing through the detector) are first applied. Further requirements on the number of decay electrons in the event are then used to isolate CCQE from $CC1\pi^+$ interactions. ν_μ CCQE events are selected by requiring the detection of a single electron (from the decay of a stopped muon) within 100 cm of the end point of the muon track [8]. Identification of the decay electron is possible because it follows the detection of the muon by a distinct time interval. ν_μ $CC1\pi^+$ interactions are identified by requiring the detection of two electrons [from the decay of the muon ($\mu^- \rightarrow e^- \nu_\mu \bar{\nu}_e$) and pion ($\pi^+ \rightarrow \mu^+ \nu_\mu, \mu^+ \rightarrow e^+ \bar{\nu}_\mu \nu_e$)], at least one of which must be within 150 cm of the end point of the muon track. The model dependence of the event selection is rather small since we require only that the μ^- and π^+ decay. After cuts and with 5.58×10^{20} protons on target, the CCQE data sample contains 193 709 events and the $CC1\pi^+$ sample 46 172, making these the largest samples collected in this energy range by more than an order of magnitude.

The CCQE and $CC1\pi^+$ reconstruction requires a detailed model of light production and propagation in the tank to predict the charge distribution for a given vertex and muon angle. The muon vertex, track angle, and energy are found with a maximal likelihood fit, with the energy being determined from the total tank charge. The neutrino energy for both samples is reconstructed from the observed muon kinematics, treating the interaction as a 2-body collision and assuming that the target nucleon is at rest inside the nucleus:

$$E_\nu = \frac{1}{2} \frac{2m_p E_\mu + m_1^2 - m_p^2 - m_\mu^2}{m_p - E_\mu + \cos\theta_\mu \sqrt{E_\mu^2 - m_\mu^2}}. \quad (1)$$

Here m_p is the mass of the proton, m_μ is the mass of the muon, m_1 is the mass of the neutron in CCQE events and of the $\Delta(1232)$ in $CC1\pi^+$, θ_μ is the reconstructed angle of the muon with respect to the beam axis (in the lab frame), and E_μ is the reconstructed muon energy.

The distributions of signal events in neutrino energy are obtained through a two step process. First, the aforementioned cuts are applied to select the $CC1\pi^+$ and CCQE samples. These samples can be characterized by the cut efficiency (the fraction of signal events in the data set that pass the relevant cuts) and the signal fraction (the fraction of events in a given sample that are in fact signal events). Second, a Monte Carlo simulation (MC) is used to predict the signal fractions and cut efficiencies; these values are

TABLE I. Predicted composition of CC1 π^+ -like (one μ^- and one π^+ in the final state) and CCQE-like (one μ^- and no pions in the final state) events.

Process	Fraction of CC1 π^+ -like events (%)	Fraction of CCQE-like events (%)
CC1 π^+ resonant	86.0	9.4
CC1 π^+ coherent	6.3	0.2
CCQE	2.4	85.4
Multipion	2.5	0.02
CC1 π^0	1.0	2.5
DIS	0.2	<0.01
Other	1.6	2.5

then used to correct the raw numbers of events passing cuts.

For our primary measurement, we define CC1 π^+ signal as events with exactly one μ^- and one π^+ escaping the struck nucleus (which we call CC1 π^+ -like events) and CCQE signal as those with exactly one μ^- and no pions (CCQE-like events). Both event classes may include any number of protons or neutrons, but no other types of hadrons. The observed cross section ratio is then defined as the ratio of CC1 π^+ -like to CCQE-like events and thus has not been corrected for reinteractions in the struck nucleus. The signal fraction of the CC1 π^+ -like (CCQE-like) sample is predicted to be 92% (83%) and the cut efficiency is predicted to be 26% (38%) in 500 cm. Table I gives the composition of the CC1 π^+ -like and CCQE-like signal events in the MC.

To map reconstructed to true energy, we form a migration matrix A_{ij} representing the number of MC events in bin i of reconstructed energy and bin j of true energy. We then normalize each reconstructed energy bin to unity to obtain an unsmearing matrix. This is equivalent to a Bayesian approach discussed in [15]; it differs from the standard matrix inversion method in that the resulting unsmearing matrix is biased by the MC distribution used to generate it. We account for this in our uncertainties by including a variation in the MC distribution used to generate the matrix. Because we have good data-MC agreement this effect is small. The advantage of this method is that it avoids the problems of numerical instability and the magnification of statistical errors which occur in matrix inversion. This unsmearing procedure also proved insensitive to variations in neutrino energy reconstruction, confirming that it performs as intended.

With all the correction terms put together, the cross section ratio in each energy bin i is:

$$\frac{\sigma_{1\pi^+,i}}{\sigma_{QE,i}} = \frac{\epsilon_{QE,i} \sum_j U_{1\pi^+,ij} f_{1\pi^+,j} N_{1\pi^+-cuts,j}}{\epsilon_{1\pi^+,i} \sum_j U_{QE,ij} f_{QE,j} N_{QE-cuts,j}}, \quad (2)$$

where subscript i runs over bins in true neutrino energy, subscript j indexes bins in reconstructed neutrino energy, N_{X-cuts} denotes the number of events passing cuts for $X = \text{CC1}\pi^+$, CCQE, f denotes a signal fraction, ϵ denotes a cut

efficiency, and U is a neutrino energy unsmearing matrix that acts on a reconstructed distribution to return the true distribution.

Figure 1 shows the observed CC1 π^+ -like to CCQE-like ratio extracted from the MiniBooNE data, including statistical and systematic uncertainties.

The systematic uncertainties on the cross section ratio arise from five main sources: the neutrino flux (which largely cancels in the ratio), the neutrino interaction cross sections (which affect the background predictions), the target nucleon momentum distribution (which accounts for the model dependence of our unfolded neutrino energy), hadron reinteractions in the detector, and the detector simulation (which describes light propagation in the oil). In the region of highest statistics (about 1 GeV), there is roughly an 8% fractional error on the ratio resulting from hadron rescattering in the detector, 6% from neutrino cross sections, 4% from the detector simulation, 2% from the nucleon momentum distribution, 2% from the neutrino flux, and 2% from the statistics of the two samples.

In addition to these errors, an uncertainty on the Q^2 dependence of the predicted CC1 π^+ cross section is as-

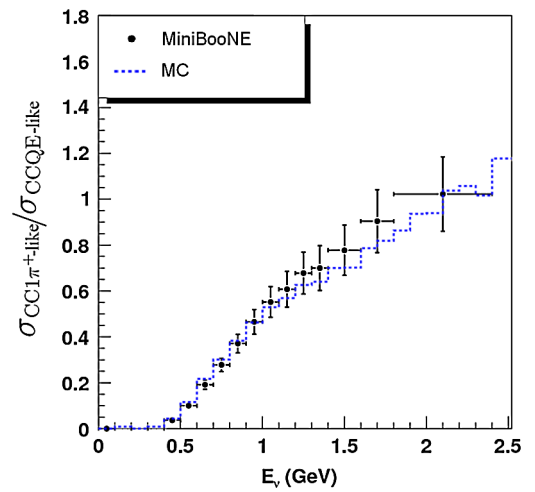


FIG. 1 (color online). Observed CC1 π^+ -like:CCQE-like cross section ratio on CH₂, including both statistical and systematic uncertainties, compared with the MC prediction [6]. The data have not been corrected for hadronic reinteractions.

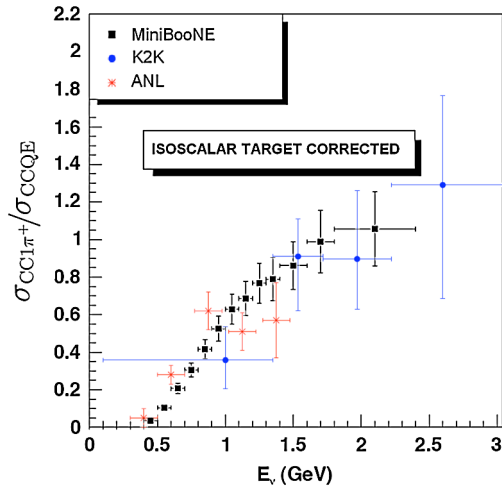


FIG. 2 (color online). FSI-corrected $CC1\pi^+$ to CCQE cross section ratio on CH_2 compared with results from ANL (D_2) [1] and K2K (C_8H_8) [3]. The data have been corrected for final state interactions and rescaled for an isoscalar target.

sessed based on comparison to MiniBooNE data. This contributes less than a 3% error to the measured ratio. Additional variations testing the sensitivity of the result to the event selection scheme, reconstruction algorithm, energy unsmearing method, and predicted π^+ momentum distribution in $CC1\pi^+$ events are also included in the total uncertainty shown in Fig. 1. Each of these contributes a 1%–2% uncertainty to the ratio at 1 GeV.

Unlike the result presented in Fig. 1, the ratio reported by all prior experimental measurements [1–3] has been one in which the effects of final state interactions (FSI) in the target nucleus have been removed using MC. Solely for the purpose of comparison, we now extract a similarly corrected value. The FSI-corrected ratio is defined as the ratio of $CC1\pi^+$ to CCQE events at the initial vertex and before

any hadronic reinteractions. Thus, the signal fractions and cut efficiencies for the FSI-corrected ratio include corrections for intranuclear hadron rescattering based on the MC’s model for nuclear effects. The measurement proceeds exactly as for the observed ratio (Fig. 1), except that now we define $CC1\pi^+$ and CCQE, rather than $CC1\pi^+$ -like and CCQE-like, events as signal for the respective samples. With these definitions, the CCQE ($CC1\pi^+$) sample has a signal fraction of 72% (87%) and a cut efficiency of 37% (20%) in 500 cm. The FSI-corrected ratio is shown in Fig. 2. The corrections for final state interactions have uncertainties associated with them, introducing additional systematic error to the cross section ratio. The fractional error on the ratio due to these corrections is roughly 6% in the region of highest statistics.

Here we limit our comparison to those experiments which reported both CCQE and $CC1\pi^+$ cross sections, using the same energy bins for each of these interactions, so as to facilitate comparison with our measured $CC1\pi^+$:CCQE ratio. Our result agrees with both Argonne National Laboratory (ANL), which used a deuterium target, and the K2K Collaboration, which used C_8H_8 (Fig. 2). In order to make this comparison, the MiniBooNE and K2K results have been rescaled to an isoscalar target. To perform this correction, we rescale the ratio by a factor of $(1 - r)s_p$, where r is the ratio of neutrons to protons in the target and s_p is the fraction of π^+ production that is predicted (by MC) to occur on protons. The resulting scaling factor is 0.80 for MiniBooNE; for K2K we use the factor of 0.89 provided in [3]. The results have not been corrected for their differing nuclear targets nor for the application of explicit invariant mass requirements (although the latter are similar). ANL used an explicit cut on invariant mass $W < 1.4$ GeV. While no invariant mass cut is used in this analysis, the MiniBooNE spectrum is such that $CC1\pi^+$ events occur only in the region $W < 1.6$ GeV;

TABLE II. The MiniBooNE measured $CC1\pi^+$ to CCQE (as in Fig. 2 but without the isoscalar correction) and $CC1\pi^+$ -like to CCQE-like (Fig. 1) cross section ratios on CH_2 including all sources of statistical and systematic uncertainty.

E_ν (GeV)	$CC1\pi^+$:CCQE (FSI corrected)	$CC1\pi^+$ -like:CCQE-like (observed)
0.45 ± 0.05	0.045 ± 0.008	0.036 ± 0.005
0.55 ± 0.05	0.130 ± 0.018	0.100 ± 0.011
0.65 ± 0.05	0.258 ± 0.033	0.191 ± 0.019
0.75 ± 0.05	0.381 ± 0.047	0.278 ± 0.028
0.85 ± 0.05	0.520 ± 0.064	0.371 ± 0.040
0.95 ± 0.05	0.656 ± 0.082	0.465 ± 0.053
1.05 ± 0.05	0.784 ± 0.100	0.551 ± 0.066
1.15 ± 0.05	0.855 ± 0.114	0.607 ± 0.077
1.25 ± 0.05	0.957 ± 0.132	0.677 ± 0.091
1.35 ± 0.05	0.985 ± 0.141	0.700 ± 0.097
1.5 ± 0.1	1.073 ± 0.157	0.777 ± 0.109
1.7 ± 0.1	1.233 ± 0.207	0.904 ± 0.137
2.1 ± 0.3	1.318 ± 0.247	1.022 ± 0.161

similarly, K2K's measurement covers the region $W < 2$ GeV [3].

The dominant reason for the difference between the ratios presented in Figs. 1 and 2 is intranuclear pion absorption in $CC1\pi^+$ events, which causes these events to look CCQE-like. As a result of π^+ absorption, a significant number of $CC1\pi^+$ events appearing in the numerator in Fig. 2 are in the denominator in Fig. 1. Thus, the FSI-corrected ratio, shown in Fig. 2, is 15% to 30% higher than the observed ratio in our energy range.

In summary, MiniBooNE has measured the ratio of $CC1\pi^+$ -like to CCQE-like events for neutrinos with energy $0.4 \text{ GeV} < E_\nu < 2.4 \text{ GeV}$ incident on CH_2 . This is the first time such a ratio has been reported. Additionally, the ratio of the $CC1\pi^+$ and CCQE cross sections at the vertex has been extracted using MC to remove the effects of final state interactions, in order to facilitate comparison with previous experimental measurements. The results are summarized in Table II. The measured ratios agree with prediction [6,9] and previous data [1,3].

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